

Neural coding: a perspective for new associative memories

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2 Our model

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- Application example

3 Direction: learning sequences

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Challenge

Context

Exponential growth of the amount of information



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User	Difficult to find the desired piece of information.
Engineer	Algorithms complexity is limiting, Ad-hoc solutions are often required.

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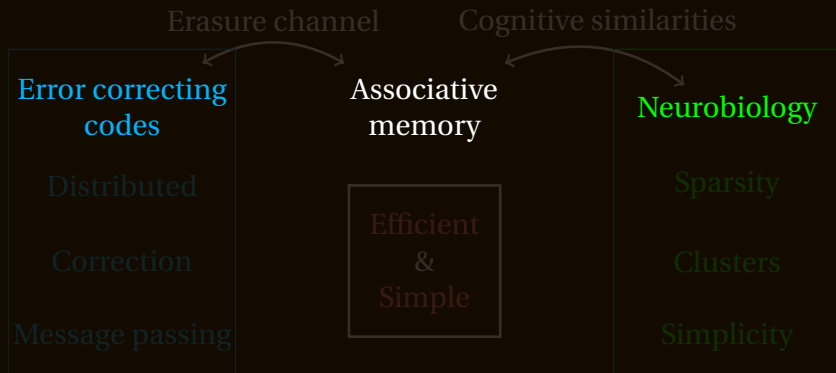
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Approach

Definition

Associative memory = device that can retrieve previously learned messages from part of them.

Idea

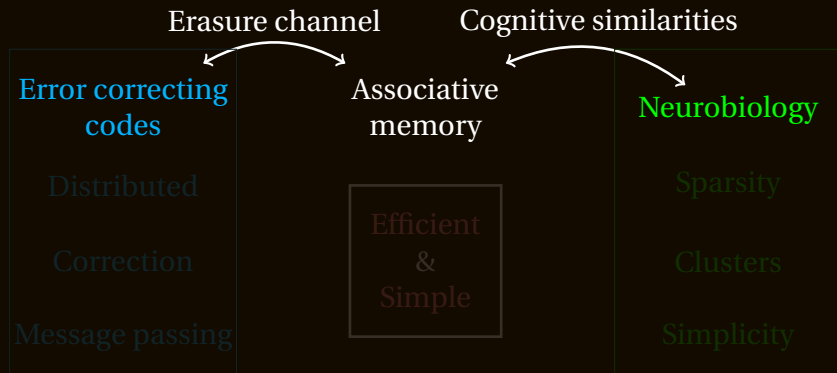


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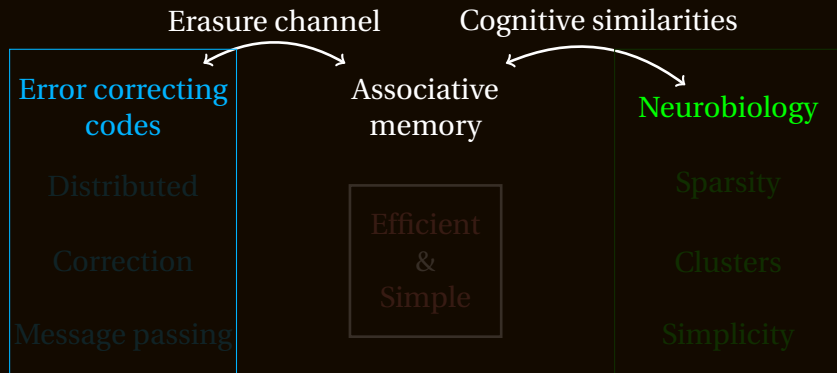


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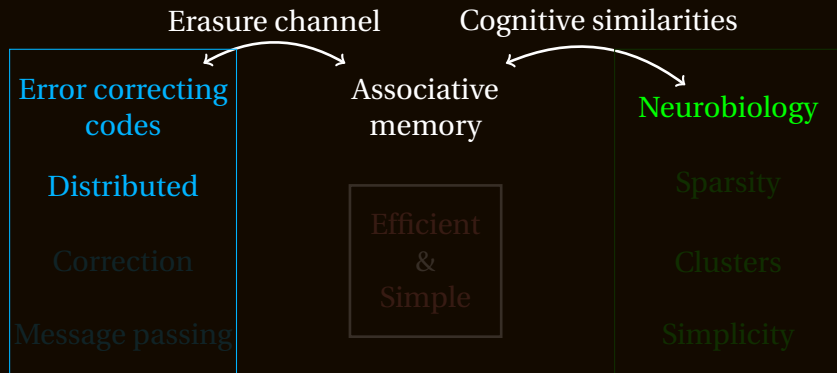


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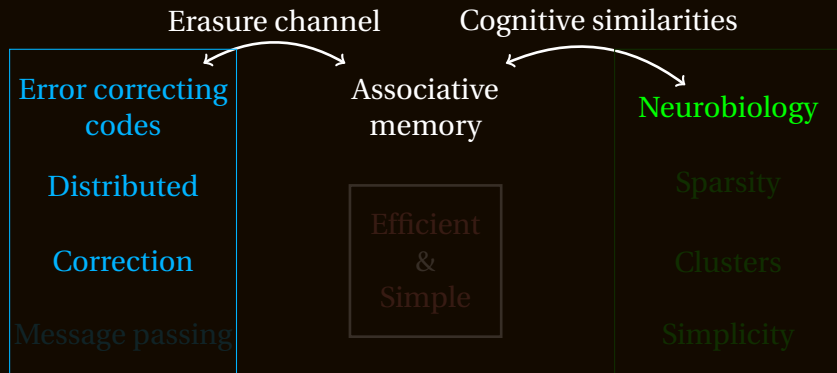


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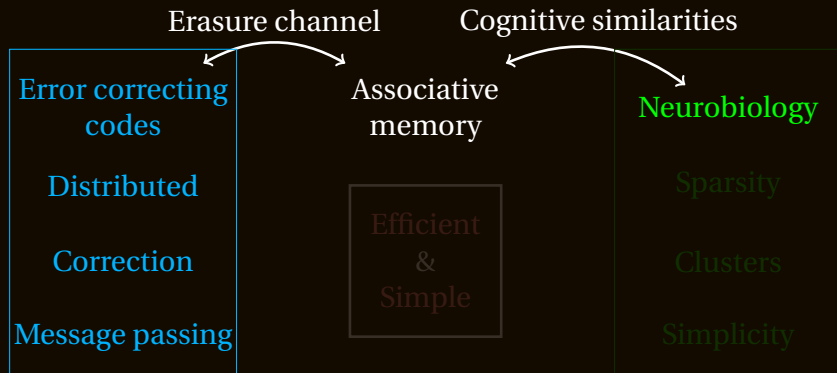


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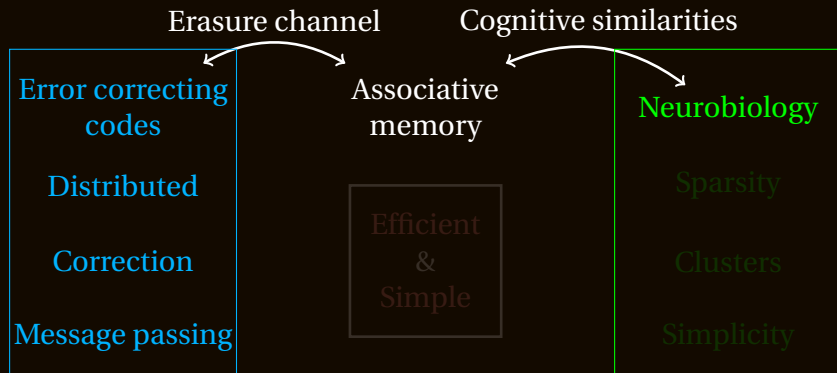


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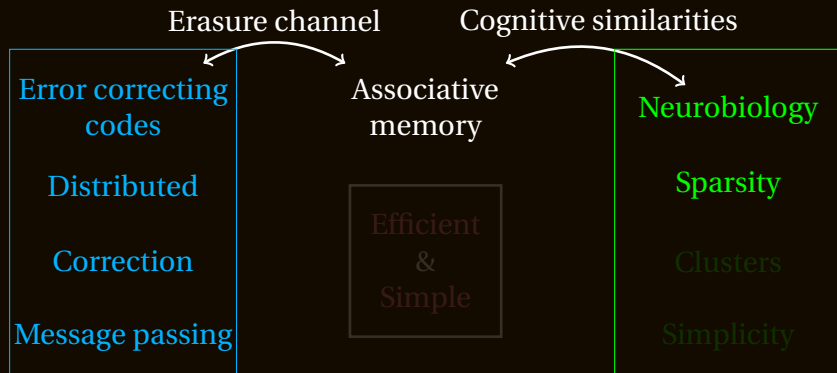


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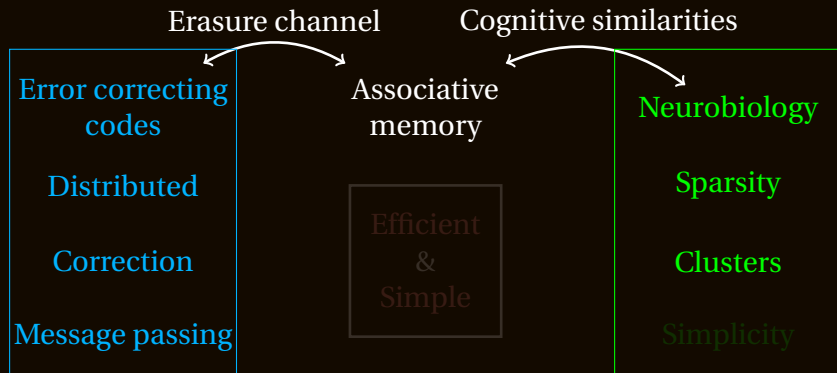


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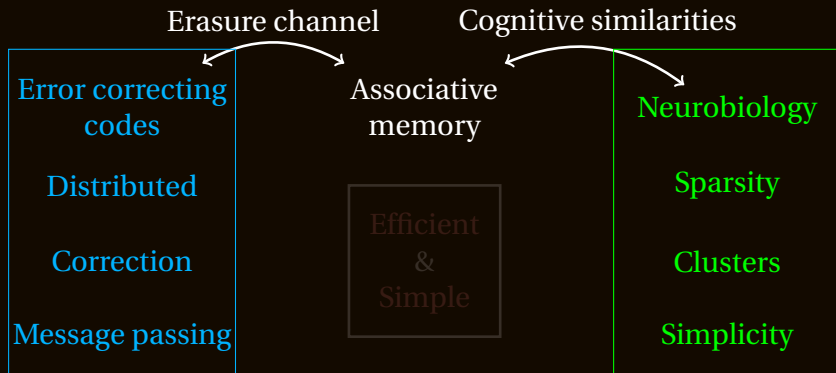


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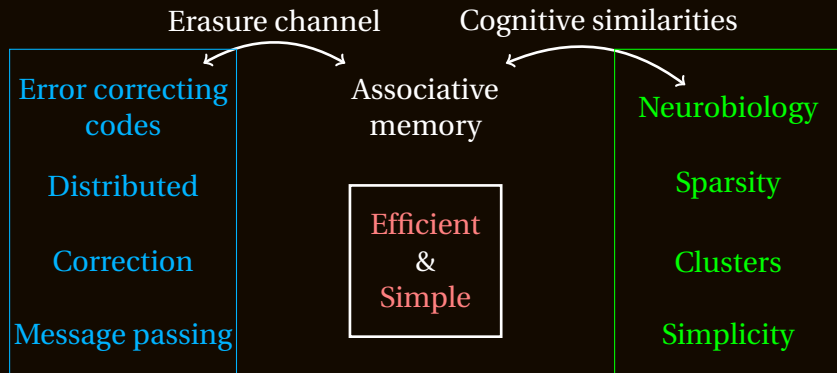


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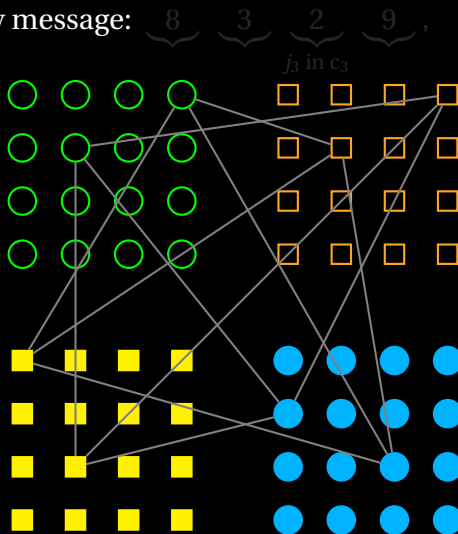
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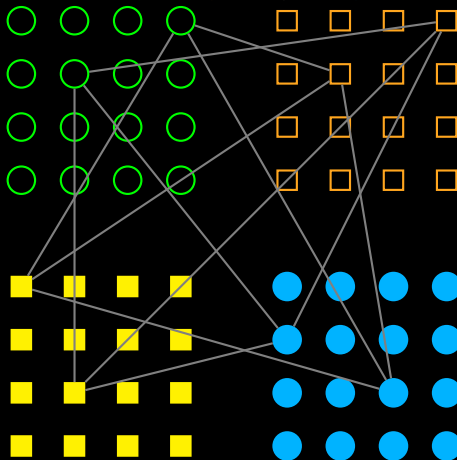
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- Example: $c = 4$ clusters made of $l = 16$ neurons each,
- Learn 16-ary message: $\{8, 3, 2, 9\}$,



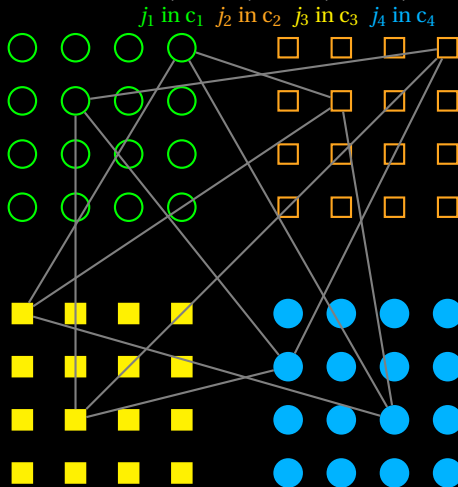
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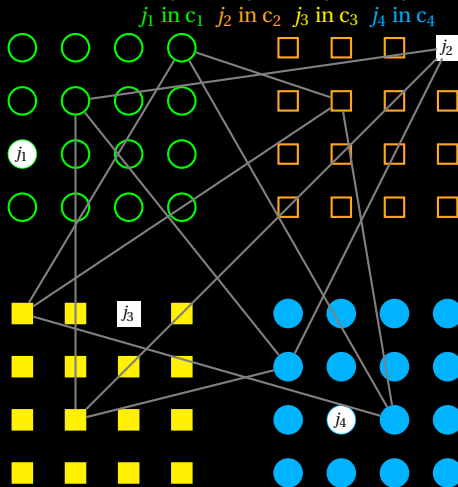
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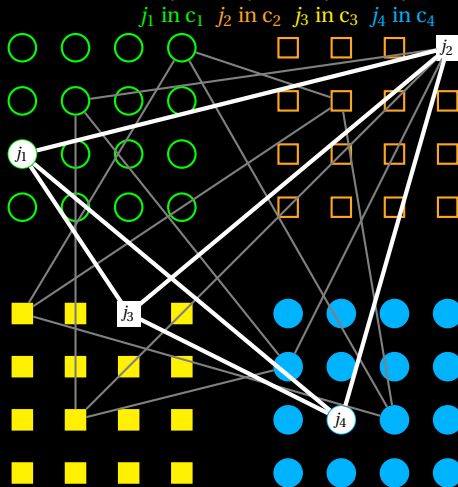
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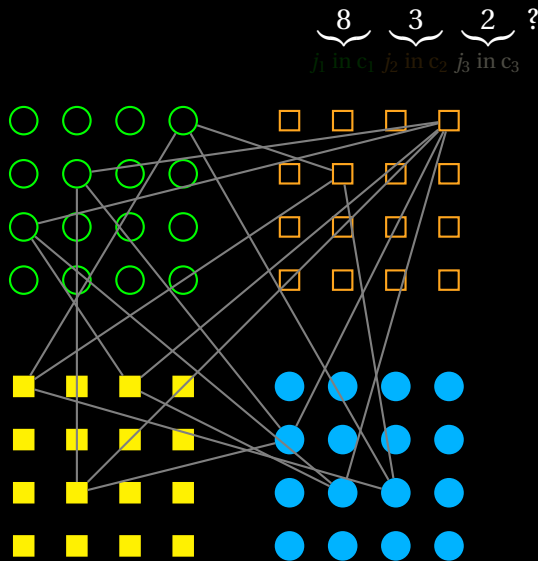


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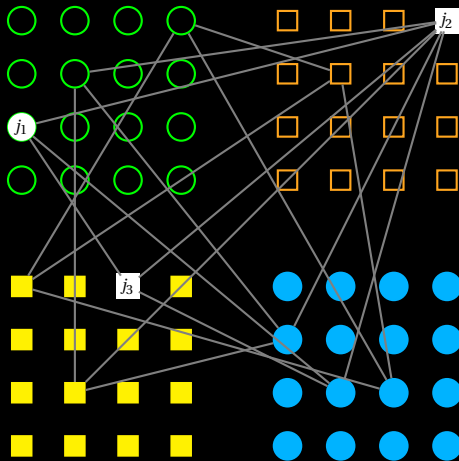


- Projection to the network,
- Global decoding: sum,
- Local decoding: winner-take-all,
- Possibly iterate the two decodings.

Our model: retrieving

$$\underbrace{\quad}_8 \quad \underbrace{\quad}_3 \quad \underbrace{\quad}_2 \quad ?$$

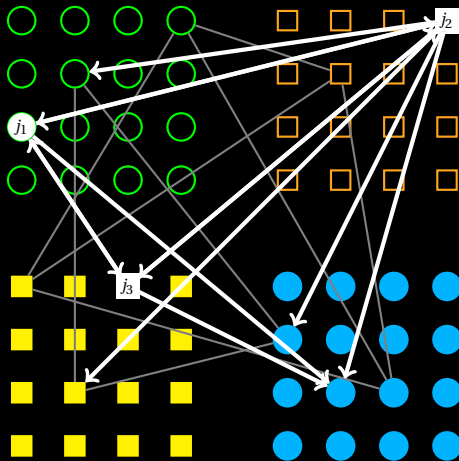
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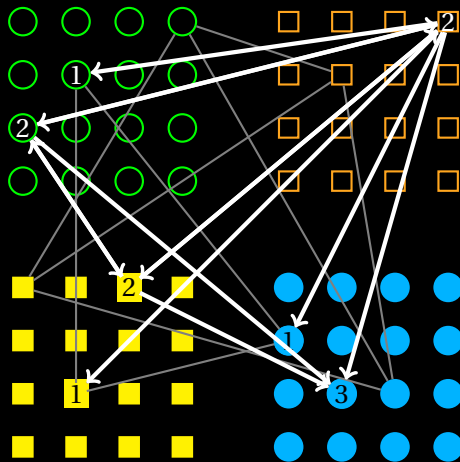
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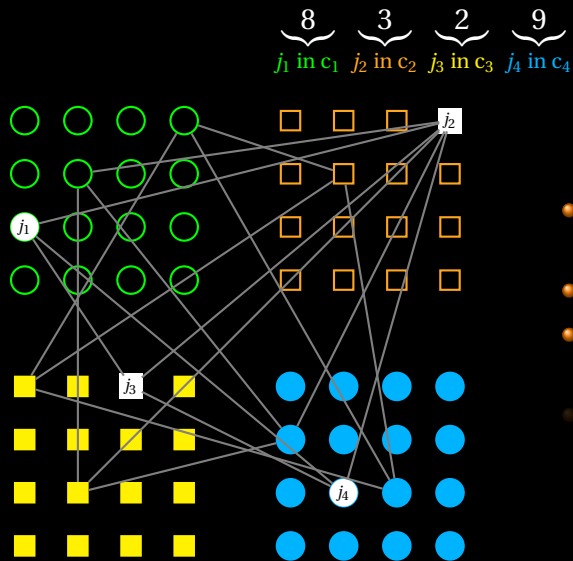
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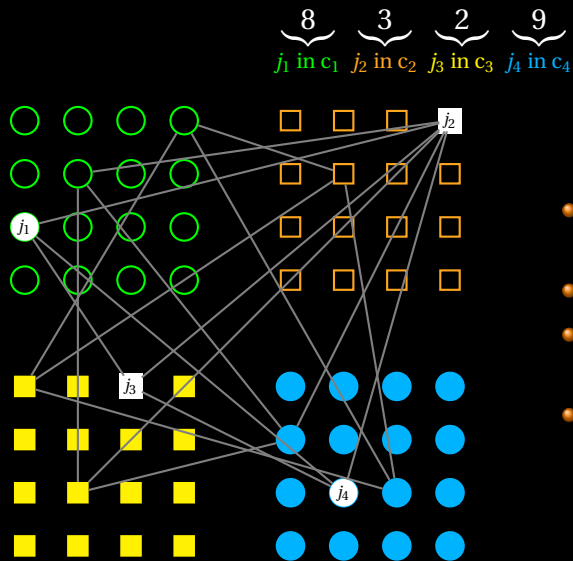
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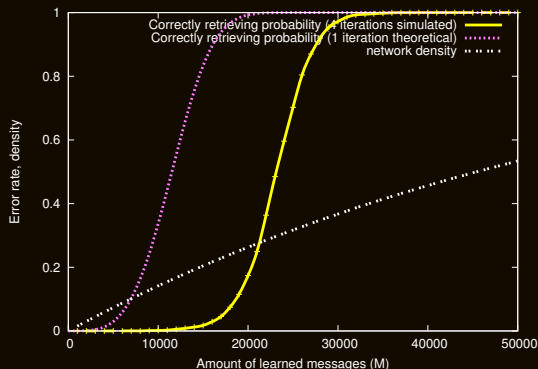
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Associative memory



$c = 8, l = 256$ neurons each. Input messages have just 4 known symbols.

State-of-the-art Hopfield network



Our network



An example: cache design

Role

Speed-up the lookup of frequently accessed data.

Context

- With associativity decreases the miss rate,
- Current implementations are limited to 8-ways associativity,
- Speed and area limitations.

Our proposal

- Adaptation of the network:
 - Given the address, find the associated data,
- Additionnal error probability: 10^{-30} ,
- Area consumption reduced by 65%,
- Pipelined architecture using a few clock cycles.

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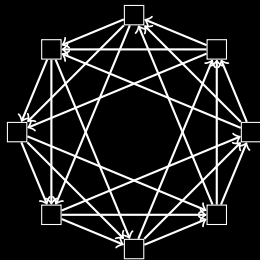
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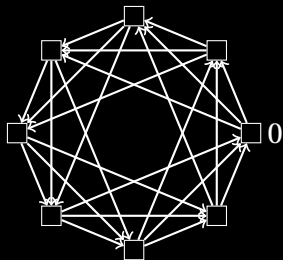


Performance

- $c = 50$ clusters,
- $l = 256$ neurons/cluster,
- $L = 1000$ symbols in sequences,
- $m = 1823$ learned sequences,
- $P_e \leq 0.01$.



Direction II: learning arbitrarily long sequences

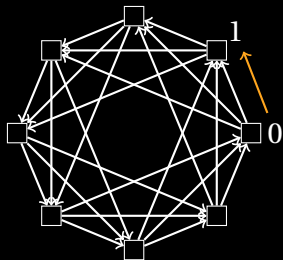


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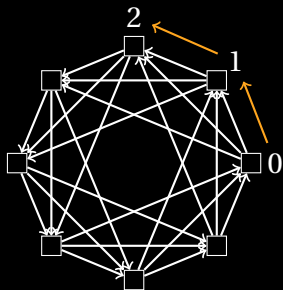


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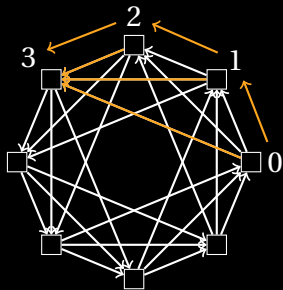


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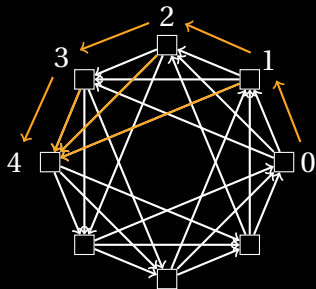


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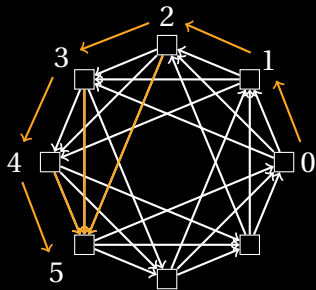


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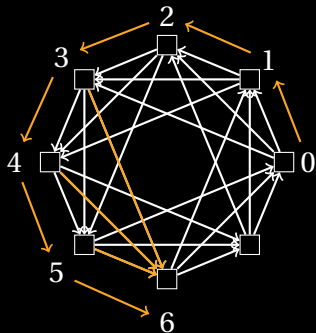


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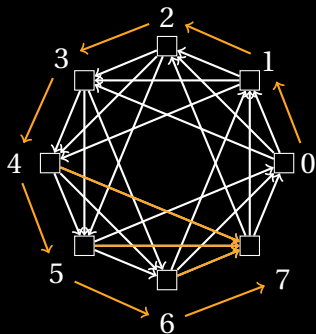


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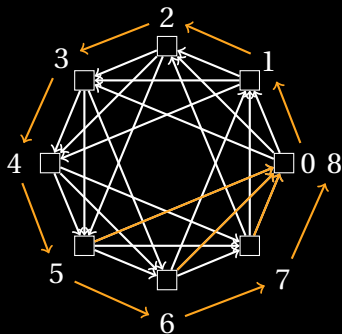


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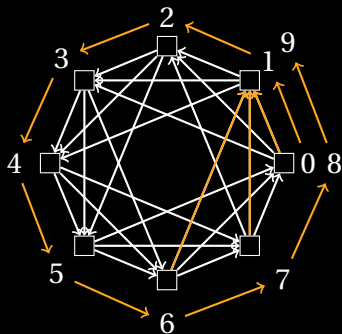


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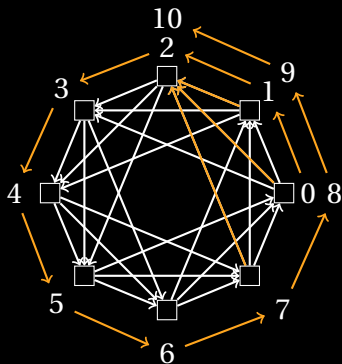


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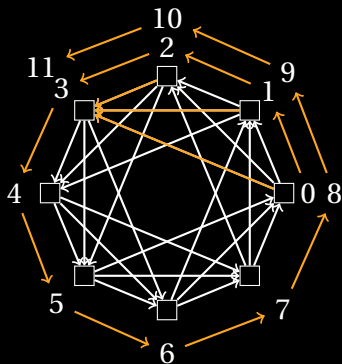


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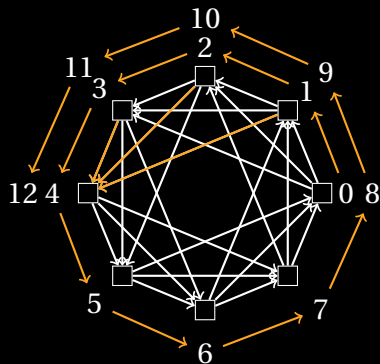


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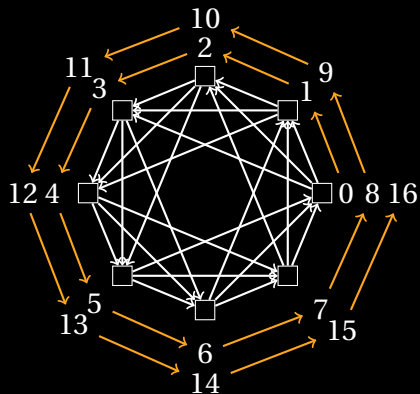


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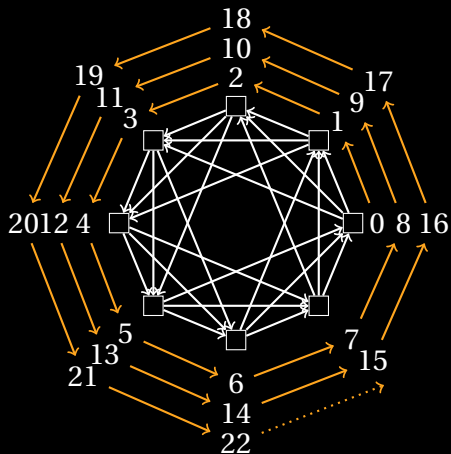


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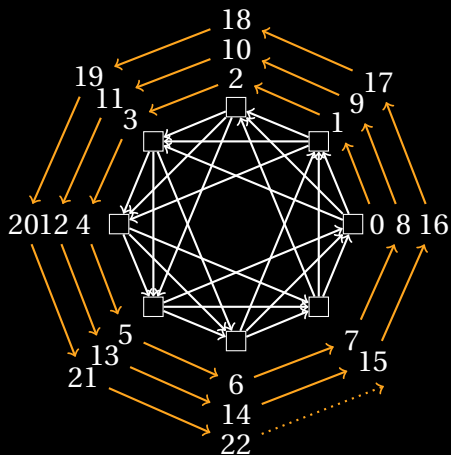


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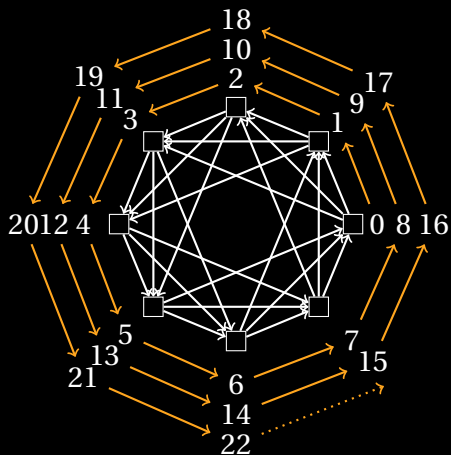


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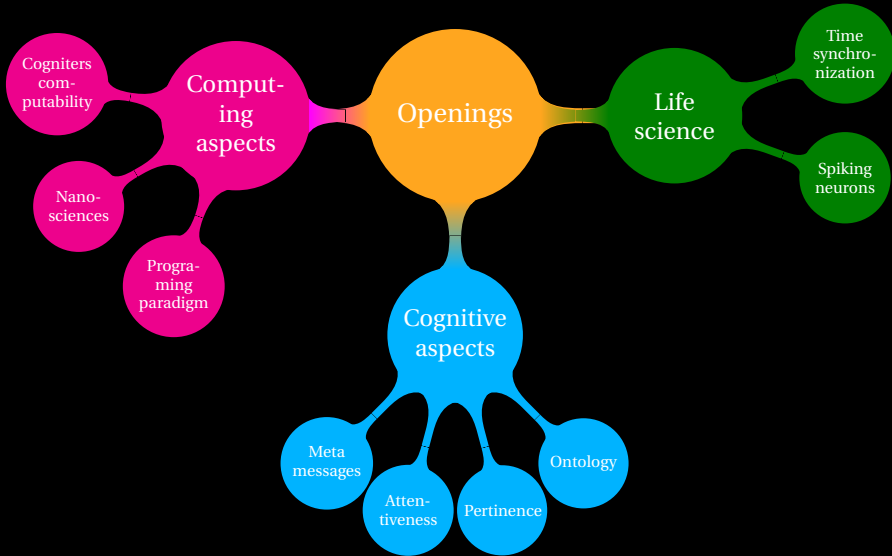
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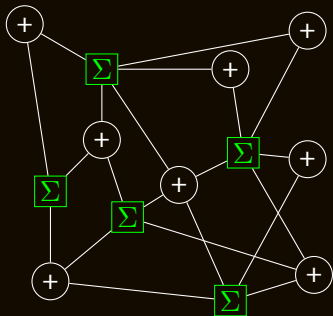
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Thank you for your attention. I am at your disposal if you have any question.

Error correcting code



Neocortical network

